Section 1.8 Absolute Value Equations

When solving an absolute value equation or inequality, it is necessary to first isolate the absolute value expression.

Objective 1: Solving an Absolute Value Equation

The absolute value of a number x, written as |x|, represents the **distance** from a number x to 0 on the number line. Consider the equation |x| = 5. To solve for x, we must find all values of x that are 5 units away from 0 on the number line. The two numbers that are 5 units away from 0 on the number line. The two numbers that are 5 units away from 0 on the number line are x = -5 and x = 5 as shown in the figure below. Therefore, the solution set for |x| = 5 is $\{-5, 5\}$.



In general, if *u* is an algebraic expression and *c* is a positive real number, then |u| = c is equivalent to u = c or u = -c.