

## Section 1.6b Other Types of Equations

### Objective 2: Solving Equations that are Quadratic in Form (“Disguised Quadratics”)

Quadratic equations of the form  $ax^2 + bx + c = 0$ ,  $a \neq 0$  are relatively straight-forward to solve since we know several methods for solving quadratics. Sometimes equations that are not quadratic can be made into a quadratic equation by using a **substitution**. Equations of this type are said to be *quadratic in form* or “*disguised quadratics*”. These equations typically have the form  $au^2 + bu + c = 0$ ,  $a \neq 0$  after an appropriate substitution.

Original Equation	Identify $u$ .	Find $u^2$ .	Make the substitutions.
$2x^4 - 11x^2 + 12 = 0$	$u = x^2$	$u^2 = (x^2)^2 = x^4$	$2u^2 - 11u + 12 = 0$
$\left(\frac{1}{x-2}\right)^2 + \frac{3}{x-2} - 15 = 0$	$u = \frac{1}{x-2}$	$u^2 = \left(\frac{1}{x-2}\right)^2$	$u^2 + 3u - 15 = 0$
$x^{2/3} - 9x^{1/3} + 8 = 0$	$u = x^{1/3}$	$u^2 = (x^{1/3})^2 = x^{2/3}$	$u^2 - 9u + 8 = 0$
$3x^{-2} - 5x^{-1} - 2 = 0$	$u = x^{-1}$	$u^2 = (x^{-1})^2 = x^{-2}$	$3u^2 - 5u - 2 = 0$